

Application of Artificial Neural Network Model in Calculation of Pressure Drop Values of Nanofluid

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ABSTRACT

Cloud computing is currently a hyped word in IT. This paper examines the capabilities and vulnerabilities of the cloud. In particular, it examines the security issues that exist in the cloud that businesses are concerned about when moving to the cloud. Steps have been taken to standardise the cloud and provide consumers with confidence in the service. The purpose of this paper is to examine some of these security issues and provide suggested alterations to the curriculum for secure programming modules in order to resolve or reduce the impact of the issues on the client.

Keywords: *Nanofluids, Particle volumetric concentration, Turbulent flow, Pressure drop, and Artificial neural network.*

NOMENCLATURE

E	sum square error
Re	Reynolds number
T	nanofluid temperature, °C
V	weight factors in the input-to-hidden connections
W	weight factors in the hidden-to-output connections
X	input set for ANN model
Y	output set of ANN model
Z	data set for hidden layers

Greek Symbols

ϕ	particle volumetric concentration, %
ΔP	pressure drop of nanofluid, kPa

Subscripts

i, j, q indices

1. INTRODUCTION

Basically, many industrial processes involve the transfer of heat by means of a flowing fluid in either the laminar or turbulent regime as well as flowing or stagnant boiling fluids. Most of these processes would benefit from a decrease in the thermal resistance of the heat transfer fluid. Correspondingly, smaller heat transfer systems with lower capital cost and improved thermal efficiencies would result. Nanofluid is the name conceived by Argonne National Laboratory to describe a fluid in which nanometer-sized solid particles, fibers, or tubes are suspended in liquids such as water, engine oil, and

ethylene glycol (EG). Nanofluids have the potential to reduce such thermal resistances and can be used in different industrial applications such as electronics, transportation, medical, food, and manufacturing of many types [1].

While thermal properties are important for heat transfer applications, the viscosity is also important in designing nanofluids for flow and heat transfer applications because the pressure drop and the resulting pumping power depend on the viscosity. Many experimental investigations on the heat transfer performance and pressure drop of different nanofluids with various nanoparticle volume concentrations in both laminar and

turbulent flow regimes have been reported [2-10]. These experimental results showed variations of the pressure drop values of the nanofluids. So far, the results of Duangthongsuk and Wongwises [2] showed that the pressure drop of nanofluids was slightly higher than the base fluid and increases with increasing the volume concentrations. Also, the results of Duangthongsuk and Wongwises [3] and He *et al.* [4] disclosed that the pressure drop of the nanofluids was very close to that of the base fluid. Ko *et al.* [5] experimentally measured the pressure drop of nanofluids containing carbon nanotubes flowing through a horizontal tube under laminar and turbulent flow conditions. Their results revealed significant increase in pressure drop on nanofluids under laminar flow condition, while, the pressure drop of nanofluids presented similar values to those of the base fluid at the turbulent flow conditions. Results show the same trend as revealed in another article published by Yang *et al.* [6] that the enhancement of pressure drop for TiO₂ nanofluid was lower under turbulent in a circular pipe but higher under laminar flow conditions. Recently, turbulent heat transfer behavior of titanium dioxide/water nanofluid in a circular pipe under fully-developed turbulent regime for various volumetric concentrations was investigated experimentally by Sajadi and Kazemi [7]. Their measurements showed that the pressure drop of nanofluid was slightly higher than that of the base fluid and increased with increasing the volume concentration. In contrast, the results of Fotukian and Esfahany [8] indicated that the maximum increase in pressure drop was about 20 % for nanofluid. In the same trend, the experimental results of Peng *et al.* [9] showed that the frictional pressured drop of refrigerant-based nanofluid increases with the increase of the mass friction of nanoparticles, and the maximum enhancement of frictional pressure drop was 20.8 % under their experimental conditions. Moreover, Vajjha *et al.* [10] reported that the pressure loss of nanofluids increases with an increase in particle volume concentrations and the increase of pressure loss for a 10 % Al₂O₃ nanofluid was about 4.7 times than that of the base fluid.

Various theoretical/numerical models were proposed to study the mechanism and predict the thermal conductivity and pressure drop of different nanofluids [11-13]. The numerical studies of nanofluids can be conducted using single-phase (homogenous) or two-phase approaches. In the former approach it is assumed that the fluid phase and nanoparticles are in thermal equilibrium with zero relative velocity. While, in the latter approach, base fluid and nanoparticles are considered as two different liquid and solid phases with different momentums respectively [11]. Some of the published articles were related to investigation of laminar convective heat transfer of nanofluids [11, 12], while, the others were concerned with turbulent ones [13]. Fard *et al.* [11] used Computational Fluid Dynamics (CFD) approach regarding single-phase and two-phase models to study laminar convective heat transfer of nanofluids with different volume concentration

in a circular tube. Their numerical results have clearly shown that nanofluids with higher volume concentration have higher pressure drop and two-phase model showed better agreement with experimental data. Commercial CFD package, FLUENT, was used by Demir *et al.* [12] for solving the volume-averaged continuity, momentum, and energy equations of different nanofluids flowing in a horizontal tube under constant temperature condition. Their numerical results have clearly indicated that pressure drop increases with increasing the particle loading parameter and Reynolds number because of increasing velocity and viscosity of nanofluid. Turbulent flow and heat transfer of three different nanofluids flowing through a circular tube under constant heat flux condition have been numerically analyzed by Namburu *et al.* [13]. They assumed and used single-phase fluid model to solve two-dimensional steady, forced turbulent convection flow of nanofluid flowing inside a straight circular tube. Two-equation turbulence model of Launder and Spalding was adopted by Namburu *et al.* [13] in their numerical analysis. Their computed results indicated that pressure loss increases with increase in the volume concentration of nanofluids.

Based on the preceding literature on both experimental and theoretical reviews, one could conclude that the variations in the experimental data of the pressure drop of nanofluids are attributed to the difficulties of the experimental studies. These difficulties due to lack in understanding the details and mechanisms of heat transfer phenomenon that increase the thermal conductivity and pressure drop in nanofluids [14]. On the other side, the algorithms employed in numerical studies particularly with turbulent flows are usually complicated since involving the solution of complex differential equations. As a corollary, these programs usually require large computer power and need a considerable amount of time to give accurate predictions. Instead of carrying experimental measurements or using complex algorithms and mathematical routines in classical methods to calculate the pressure drop in a pipe under turbulent regime, a simple and accurate model is needed.

The objective of this study is to develop an Artificial Neural Network (ANN) model to calculate the pressure drop values of nanofluid at different particle volumetric concentrations, nanoparticle diameters, nanofluid temperatures and different values of Reynolds number. Titanium dioxide dispersed in water (TiO₂-water) was selected as a nanofluid due to their available experimental data to assess the proposed ANN model.

2. ARTIFICIAL NEURAL NETWORK (ANN) PRINCIPLES

2.1 ANN Model Structure

Artificial neural networks are computational model constructed of many simple interconnected elements called neurons, which is based on the information

processing system of the human brain. Fig. 1. shows the architecture of the neural network model used in this work. The basic structure is a multilayer ANN model where the chosen four inputs are fed into the first layer of hidden units. There, the circles represent the neurons (weights, bias, and activation functions) and the lines represent the connections between the inputs and neurons, and between the neurons in one layer and those in the next layer. Several studies have found that a three-layered neural network, where there are three stages of neural processing between the inputs and outputs, can approximate any nonlinear function to any desired accuracy [15-17]. Each layer consists of units which receive their input from units from a layer directly below and send their output to units in a layer directly above the unit. Each connection to a neuron has an adjustable weighting factor associated with it. The output of the hidden units is distributed over the next layer of hidden units, until the last layer of hidden units, of which the outputs are fed into a layer of no output units. Training of the ANN model typically implies adjustments of connection weights and biases so that the differences between ANN outputs and desired outputs are minimized.

2.2 Back-Propagation Training Algorithm

Back-propagation training, used in this investigation, is one of the most popular ANN training methods. The basic back-propagation algorithm adjusts the weights in the steepest descent direction (negative of the gradient). This is the direction in which the error decreases most rapidly. To explain the back-propagation rule in detail, the three-layer network shown in Fig. 1. will be used. The training phase is divided into two phases as follows:

- **Forward-propagation phase:** In the first phase, input data are sent from the input layer to the output layer, i.e., $X=[X1:X4]$ is propagating from the input layer to the output layer Y.

$$Z_q = f\left(\sum_j V_{qj} X_j\right) \quad (1)$$

$$Y_i = f\left(\sum_q W_{iq} Z_q\right) \quad (2)$$

where W_{iq} and V_{qj} represent weights in the hidden-to-output and input-to-hidden connections, respectively.

- **Back-propagation phase:** In the second phase, the errors between target outputs, y , and predicted outputs, d , are calculated and propagated backwardly

to the input layer in order to change the weights of hidden layers by using the gradient descent method.

The algorithm tries to minimize the objective function, i.e. the least square error between the predicted and the target outputs, which is given by:

$$E = \frac{1}{2} \sum_p (d_o^p - y_o^p)^2 \quad (3)$$

Where p represents the number of training datasets and o represents the number of output nodes. Then the algorithm uses the steepest-descent direction to adjust the weights in the hidden-to-output and input-to-hidden connections and as follows:

$$\Delta W_{iq} = -\lambda \frac{\partial E}{\partial W_{iq}}, \Delta V_{qji} = -\lambda \frac{\partial E}{\partial V_{qji}} \quad (4)$$

where λ is the learning rate.

Since this algorithm requires a learning rate parameter to determine the extent to which the weights change during iteration, i.e., the step sizes, its performance depends on the choice of the value of the learning rate. The two phases are iterated until the performance error decreased to certain small range [15-17].

2.3 Activation Functions

Activation functions are used in ANNs to produce continuous values rather than discrete ones. The activation functions used in hidden layer neurons are tan sigmoid functions and the piecewise linear activation function is used for the last layer neurons. The logistic activation function or more popularly referred to as the sigmoid function is semi-linear in character, differentiable and produces a value between 0 and 1. The mathematical expression of this sigmoid function is:

$$f(net_j) = \frac{1}{1 + e^{-c(net_j)}} \quad (5)$$

where c controls the firing angle of the sigmoid. When c is large, the sigmoid becomes like a threshold function and when c is small, the sigmoid becomes more like a straight line (linear). When c is large learning is much faster but a lot of information is lost, however when c is small, learning is very slow but information is retained. Because this function is differentiable, it enables the back-propagation algorithm to adapt the lower layers of weights in a multilayer neural network.

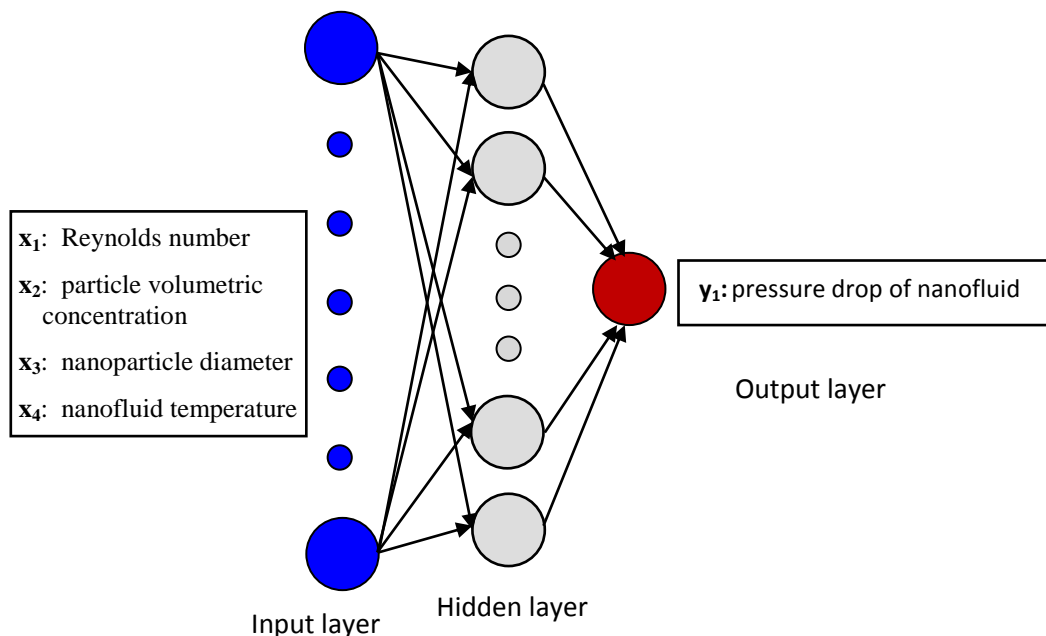


Fig. 1. A schematic of neural network model

Table 1: The range of input parameters used in training and testing the proposed ANN model [2-4]

Input variable	Duangthongsuk and Wongwises [2]	Duangthongsuk and Wongwises [3]	He et al. [4]
Reynolds number range	3800 – 12300	4000 – 16400	2300 – 6000
Particle volumetric concentration, ϕ	0 %, 0.2 %, 0.6 %, 1.0 %, 1.5 %	0 %, 0.2 %	0 %, 0.24 %, 0.6 %
Nanoparticle diameter	21 nm	21 nm	95 nm
Nanofluid temperature	15 °C	15, 20, 25 °C	22 °C

3. ANN MODEL

In the present study, the effects of four independent quantities on the pressure drops of Titanium dioxide dispersed in water (TiO₂-water) flowing through a pipe under turbulent flow regime is investigated. These four independent quantities are the particle volumetric concentration in nanofluid, temperature of nanofluid, nanoparticle diameter, and Reynolds number of flow. Therefore, the values of these four inputs are fed into the hidden layer. Each connection to a neuron has adjustable weighting factor associated with it. The outputs of the hidden layer are fed into a layer of one output units which is the pressure drop ΔP of nanofluid. The activation functions in hidden layer neurons are tan sigmoid functions and the piecewise linear activation function is used for the last layer neurons. The algorithm tries to minimize the objective function, i.e. the least square error

between the predicted and the target outputs. Several neural network models were trained with various design including number of hidden layers and number of nodes in each hidden layer. The selection of the optimum model was based on minimizing the difference between the neural network results and the desired output. It was found that, best structure of the ANN model has an input layer, a hidden layer and an output layer. Therefore, the developed ANN architecture has a configuration as shown in Fig. 1. The input layer comprises all of the four input variables, which are connected to neurons in the hidden layer through the weights assigned for each link. The number of neurons in the hidden layer is found by optimizing the network. All the four input parameters and their range of values of Titanium dioxide dispersed in water (TiO₂-water) used to develop the neural network model are mentioned in Table 1[2-4].

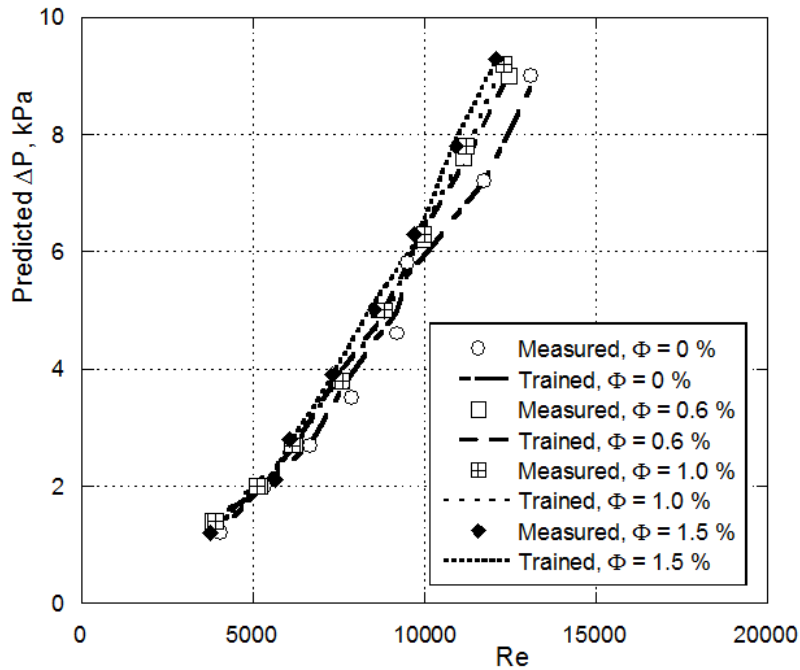


Fig. 2. Comparison of ANN-predicted values of pressure drop ΔP with Reynolds number Re for the training data set for 21 nm nanoparticle at 15 °C nanofluid temperature

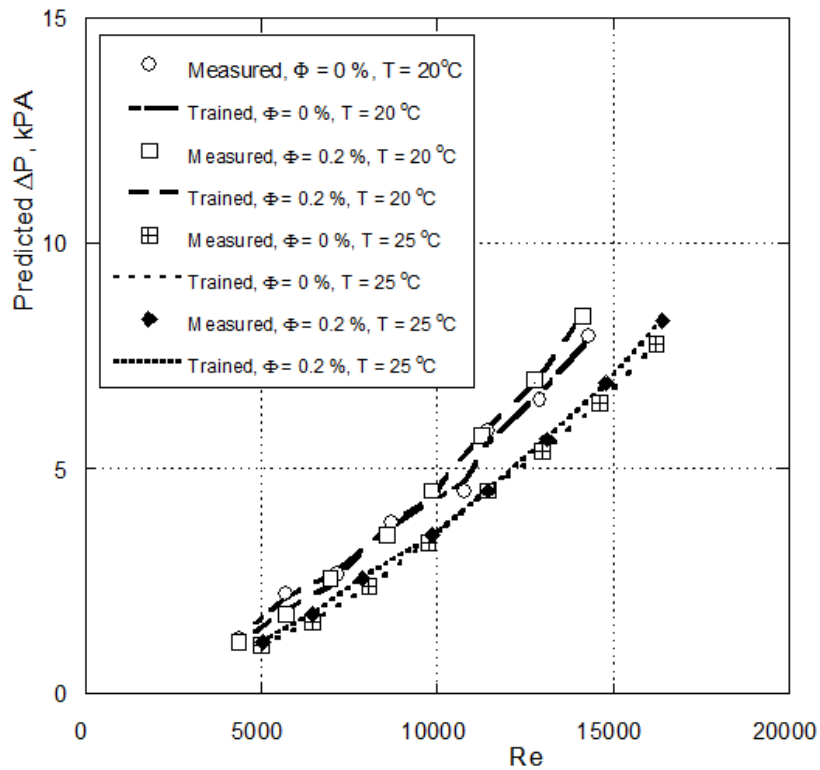


Fig. 3. Comparison of ANN-predicted values of pressure drop ΔP with Reynolds number Re for the training data set for 21 nm nanoparticle at 20 °C and 25 °C nanofluid temperatures

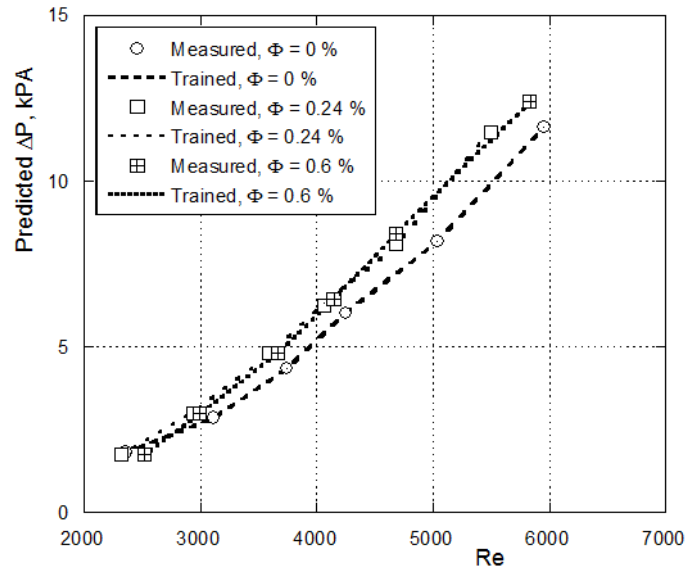


Fig. 4. Comparison of ANN-predicted values of pressure drop ΔP with Reynolds number Re for the training data set for 95 nm nanoparticle at 22 °C nanofluid temperature

4. RESULTS OF VALIDATION

A set of experimental data (16 values) of Duangthongsuk and Wongwises [3] for 21 nm nanoparticle of TiO_2 dispersed in water at 15 °C nanofluid temperature was used to validate the proposed ANN model. In Fig. 5, the predicted results of pressure drop, ΔP , from the ANN model are compared to the experimental measured data of Duangthongsuk and Wongwises [3]. What has to be noticed from Fig. 5 is that the predicted values of pressure drop are in excellent agreement with the experimental data of Duangthongsuk and Wongwises [3]. To evaluate

the accuracy of the ANN model predictions, figure 6 shows another prediction performance measurement which a straight line indicating the perfect prediction is provided. Note that in Figs. 5 and 6, the comparisons were made using the experimental values only from the test data set, which was not introduced to the ANN model during the training process as mentioned before and was selected randomly from experimentally obtained data set of Duangthongsuk and Wongwises [3]. It can be seen in Fig. 6. that the predicted results of pressure drop mimics almost the corresponding experimental results.

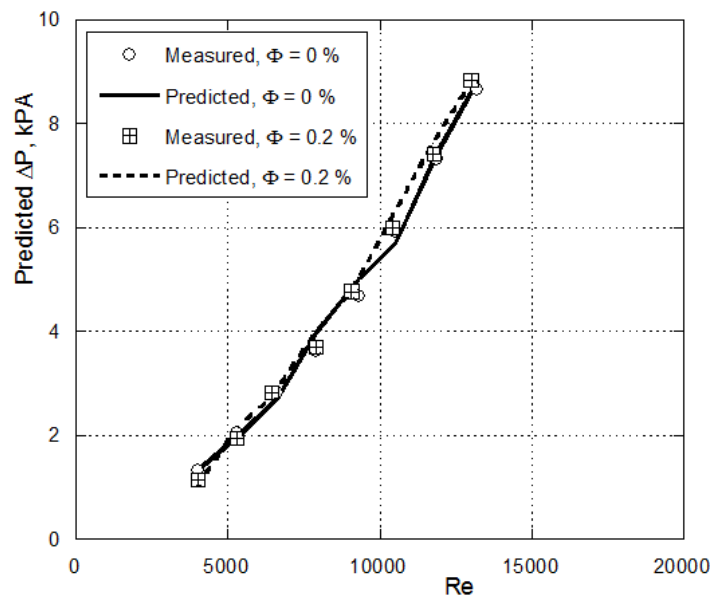


Fig. 5. Comparison of ANN-predicted values of pressure drop ΔP with Reynolds number Re for

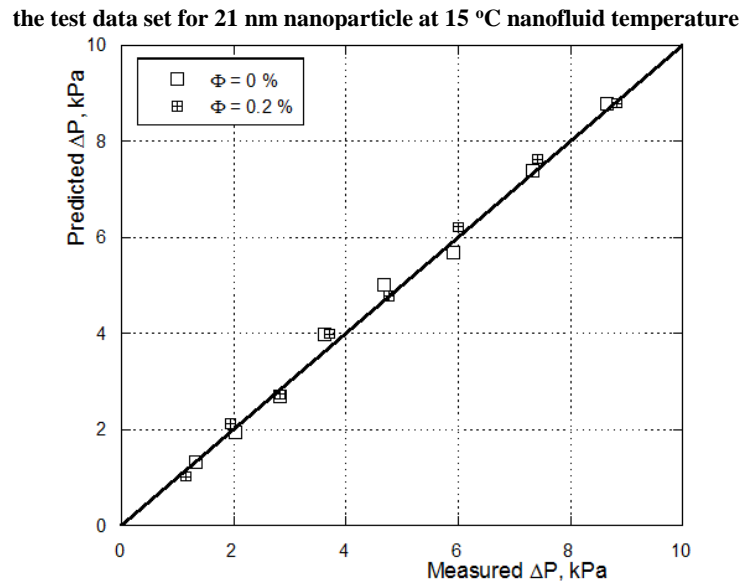


Fig. 6. Comparison of experimentally measured and ANN-predicted values of pressure drop ΔP for the test data set for 21 nm nanoparticle at 15 °C nanofluid temperature

5. CONCLUSION

An ANN model to predict the pressure drop of TiO₂-water flowing through a horizontal pipe under different turbulent flow conditions has been proposed in this study. Different experimental measured data with different particle volumetric concentrations, nanoparticle diameters, and nanofluid temperatures at different values of Reynolds number were used to construct the present ANN model. The ANN model based on a multilayer perception with back propagation learning algorithm was developed. Excellent agreement between the predicted values and the experimental data at different parameters for pressure drop of TiO₂-water nanofluid was clearly noticed. More experimental measured data for other nanofluids are needed to widen the range of application of the proposed ANN model, and that will be the subject of a future study.

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